Моделирование задач статистической механики методом отжига популяций

Lev Shchur

Landau Institute for Theoretical Physics
and
National Research University Higher School of Economics
Outline

1. HPC
2. ECP
3. INCITE
4. TOP500.org and top50.ru
5. Parallel annealing
6. Discussion
7. Examples
The big challenge for scientific computing is to develop algorithms and computational frameworks using the parallel architecture efficiently.

There are two approaches:

- Develop a universal framework which potentially is fully scalable;
- Invent an algorithm which is efficient for the particular set of problems.
There are two approaches:

- Invent an algorithm which is efficient for the particular set of problems and covers the broad range of problems

For example, *Population Annealing*


*J. Machta, Phys Rev E 82 (2010) 690*

*Barash, Weigel, Borovsky, Janke, LS, Computer Physics Communications 217 (2017) 341*

Can be applied to any system with the partition function
Population annealing
Population annealing with weighted averages: A Monte Carlo method for rough free-energy landscapes

J. Machta

Department of Physics, University of Massachusetts, Amherst, Massachusetts 01003, USA and Santa Fe Institute, 1399 Hyde Park Road, Santa Fe, New Mexico 87501, USA

(Received 4 June 2010; published 18 August 2010)
Population Annealing algorithm by Machta (PAM)

Partition function ratio $Q(\beta_k, \beta_{k-1})$ is given by

$$Q(\beta_k, \beta_{k-1}) = \frac{\sum_{j=1}^{\tilde{R}_{\beta_k}} \exp \left[ - (\beta_{k-1} - \beta_k) E_j \right]}{\tilde{R}_{\beta_k}}$$  \hspace{1cm} (1)$$

and normalized weights $\tau_j(\beta_k, \beta_{k-1})$ calculated accordingly by

$$\tau_j(\beta_k, \beta_{k-1}) = \frac{\exp \left[ - (\beta_{k-1} - \beta_k) E_j \right]}{Q(\beta_k, \beta_{k-1})}$$  \hspace{1cm} (2)$$

and

$$\tilde{R}_{\beta_k} = \sum_{j=1}^{\tilde{R}_{\beta_k}} \tau_j(\beta_k, \beta_{k-1}).$$  \hspace{1cm} (3)$$

$$-\beta_k \tilde{F}(\beta_k) = \sum_{i=K}^{k+1} \ln Q(\beta_k, \beta_{k-1}) + \ln \Omega$$
Population Annealing algorithm and 1\textsuperscript{st} order PT

Population Annealing algorithm and 1st order PT


\[ \beta_t = \ln(1 + \sqrt{q}) \]

\[ -\beta_k \tilde{F}(\beta_k) = \sum_{i=K}^{k+1} \ln Q(\beta_k, \beta_{k-1}) + \ln \Omega \]
Population Annealing algorithm and 1st order PT

Population Annealing algorithm and 1st order PT

Population Annealing algorithm and 1st order PT

Barzegar, Pattison, Wang, Katzgraber, PRE 98, 053308, 2018

**Algorithmic accelerators**
- Wolff cluster updates
- Houdayer cluster updates

**Implementation optimization**
- Dynamic population sizes
- Schedule optimization
- Spin selection methods
- Number of temperatures optimization

**Population Annealing**

**Parallel implementation**
- OpenMP
- MPI
FIG. 10: Scaling of the total wall time as a function of the number of processors $N$ for two system sizes $L = 8$ and $L = 12$. Launching and initialization time are not included. Note that the efficiency becomes better for larger and harder problems. For $L = 12$, the scaling remains $1/N$ up to about 1000 processors. The efficiency then decreases when the time for collecting observables becomes dominant. Note that resampling still takes a relatively small time.
Fig. 1. Diagrammatic representation of the mapping of thread blocks to spins in the updating kernel. The code works with thread blocks of size EQ\textit{threads}. Each block works on a single replica of the population, using its threads to update tiles of size 2 \times EQ\textit{threads} spins. To this end, it flips spins on one checkerboard sub-lattice first, moving the tiles over the lattice until it is covered, synchronizes and then updates the other sub-lattice.
Population Annealing algorithm and 1st order PT

Barash, Weigel, Borovsky, Janke, LS - CPC. 220 (2017) 341
1. HPC in crisis
2. Emergence of HPC facilities-as-service
3. Emergence of Big Data development
4. Quantum devices and synergy with HPC
5. New algorithms and approaches are necessary to keep scientific HPC alive
Моделирование задач статистической механики методом отжига популяций

Lev Shchur

Landau Institute for Theoretical Physics
and
National Research University Higher School of Economics